Policy and newly confirmed cases universally shape the human mobility during COVID-19

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Abstract: Understanding how human mobility pattern changes during the COVID-19 is of great importance in controlling the transmission of the pandemic. This pattern seems unpredictable due to the complex social contexts, individual behaviors, and limited data. We analyze the human mobility data of over 10 million smart devices in three major cities in China from January 2020 to March 2021. We find that the human mobility across multi-waves of epidemics presents a surprisingly similar pattern in these three cities, despite their significant gaps in geographic environments and epidemic intensities. In particular, we reveal that the COVID-19 policies and statistics (i.e., confirmed cases) dominate human mobility during the pandemic. Thus, we propose a universal conditional generative adversarial network based framework to estimate human mobility, integrating COVID-19 statistics and policies via a gating fusion module. Extensive numerical experiments demonstrate that our model is generalizable for estimating human mobility dynamics accurately across three cities with multi-waves of COVID-19. Beyond, our model also allows policymakers to better evaluate the potential influences of various policies on human mobility and mitigate the unprecedented and disruptive pandemic.

Keywords: COVID-19, human mobility, generative adversarial network

INTRODUCTION

Backgrounds. The outbreak of unprecedented global pandemic coronavirus disease 2019 (COVID-19) has spread to over 200 countries and continued to ravage the world, leading to over 200 million infections and 4 million deaths [1] around the world. Modern cities with high population density and frequent commuting are natural hotbeds for virus transmission. What’s worse, the threats from COVID-19 are far from disappearing. Nowadays, a new wave of COVID-19 Delta variant [2], appearing to cause more severe illness and be highly infectious, has wreaked havoc across the world again. The daily confirmed cases soar to 200,000 in the U.S. even after over 188 million vaccination [3]. These horrific phenomena remind us to rethink whether herd immunity can protect us considering the rapid virus mutations.

On the other hand, non-pharmaceutical interventions (NPIs) [4] have proven their effectiveness in controlling the transmission of COVID-19 in many countries [4]. For example, Wuhan, the first city attacked by
COVID-19 in China, suffered a drastic increase of tens of thousand confirmed cases, nearly overwhelming the local health care system [5]. The Chinese government successfully contained the epidemic in Wuhan and pushed the confirmed cases to zero (i.e., Zero-COVID strategy [6]) by strict lockdown and mobility restrictions, which prevent the other areas in China from the invasion of the epidemic.

Despite the superiority of mobility restrictions in cutting down the spread of COVID-19 and decreasing infection risks shown in Figure 1B, plenty of studies also discuss the negative effects of mobility restrictions on the economics [7–9], especially the brick-and-mortar business [10]. Consequently, the governments always face the dilemma in adopting strict mobility restrictions for public health [11] and economic recession, which is criticized by the media on either too late or early, too strict or loose policies [12]. Furthermore, there also have been a lot of previous studies pointing out that the human mobility level can forecast the trends of COVID-19 in China, Italy, and the U.K. [13–15] and potentially affect the economic [16, 17]. Therefore, it is imperative to model and estimate human mobility response under different mobility restriction policies, enabling the government to better control the epidemic transmission and adapt interventions during the pandemic. However, accurately predicting human mobility during COVID-19 is challenging for several reasons. First, the human mobility depends on complicated multi-scale dynamics, which is associated with varied sociodemographic characters [18], geographical conditions [19], available transportation and travel options [20]. Second, long-term epidemic-related prevention and control policies may have thoroughly re-shaped the human mobility patterns and are still ongoing [21–23], leading to inconsistency compared with the normal history data. Third, the data availability also limits the related research on human mobility considering the COVID-19 itself is a Black Swan event.

Observations and hypotheses. We utilize the anonymous human mobility data conforming to the privacy standards uploaded by the smart devices, ranging from January 1, 2020 to March 31, 2021 of three cities, Beijing (BJ), Dalian (DL), and Shijiazhuang (SJZ), of China. We can thereby comprehensively analyze and compare the human mobility dynamics of multi-waves COVID-19 across cities. Specifically, we aggregate the human mobility (i.e., the sum of regional visits) of Beijing per week, which is shown in Figure 1A, which has undergone two waves of epidemics during 2020. The deeper colors (e.g., bright regions) of the heatmap indicate higher human mobility levels. Intuitively, there are very likely to exist similar patterns from decline to revival for each wave of COVID-19, considering the Chinese government carries out the Zero-COVID strategy from the beginning to the end. Our dataset is valuable for understanding how the Zero-COVID strategy affected human mobility dynamics and eliminated the COVID-19 in China.

Nevertheless, estimating the human mobility changes for the next wave of COVID-19 across cities is still challenging due to the significantly distinct patterns in geographical terrain situations and epidemic intensity (see Supplementary Material, extended Figure 1), let alone the very limited mobility data available. The latest research reveals strong correlations between COVID-19 transmission and human mobility changes [24]. In other words, it is very probable that COVID-19 related factors potentially influence the shift of human mobility levels. To better answer this question, we dive into the underlying logic that drives the change of human mobility depicted in Figure 1C, where the human mobility, policy, and COVID-19 statistics are tightly coupled. Specifically, the COVID-19 statistics largely reshape human mobility by directly leading to strict policies on social distancing or implicitly influencing people’s willingness to travel. Then, the reshaped human mobility affects both epidemic control and economic status. There are three frequently used COVID-19 statistics, i.e., newly confirmed cases, cured cases, and death cases. To identify the principal
During lockdown
Before mobility restriction
Reopen
Before lockdown
Reopen
During mobility restriction
Date

First wave—nationwide transmission
Second wave—local transmission

Date

High population density
Low population density

Social distancing

Epidemic control
COVID-19 statistics
Policy
Economic status

Figure 1 Problem overview. (A) Human mobility changes before, during, and after the lockdown or mobility restriction policies in Beijing, China. The bright regions represent a higher human mobility level compared with the dark regions. (B) Effects of mobility restriction and social distancing in mitigating COVID-19 transmission. (C) Relations among COVID-19 statistics, policy, and human mobility.

factors influencing human mobility, we normalize the human mobility level based on the first week of 2020 to remove the impacts from city attributes (e.g., scale and layouts). Then we plot corresponding trends along with COVID-19 statistics in Figure 2. We notice that the human mobility dynamics is highly correlated with the newly confirmed cases and mobility restriction policies [25] during the pandemic (see Supplementary Material, extended Figure 2). At the same time, the curves of dead and cured patients are delayed with fewer influences on human mobility. This phenomenon is also consistent with the actual situations, e.g., the burst increase of confirmed cases usually points to the beginning of strict lockdown or mobility restrictions, resulting in a sudden drop in human mobility level. Also, suppose there are no new confirmed cases for several consecutive weeks. In that case, human mobility will revive due to fewer mobility restrictions and people’s more willingness to travel in the city [26].

Related work. There exist plenty of studies investigating the interplay among policy, human mobility,
Figure 2  Interplay between human mobility level and confirmed cases across multiple cities. (A) Beijing mobility level, along with two waves of COVID-19, the first wave from January 19, 2020 to April 30, 2020, and the second wave from June 11, 2020 to August 6, 2020. (B) Dalian mobility level, along with three waves of COVID-19, the first wave from January 19, 2020 to April 30, 2020, the second wave from July 22, 2020 to August 30, 2020, and the third wave from December 16, 2020 to January 24, 2021. (C) Shijiazhuang mobility level, along with two waves of COVID-19, the first wave from January 19, 2020 to April 30, 2020, and the second wave from January 12, 2021 to February 10, 2021.
and epidemic dynamics [24, 27, 28]. Chinazzi et al. [27] investigated the effects brought by travel restriction and revealed that travel quarantines strongly delayed the nationwide COVID-19 transmission. Lai et al. [29] claimed that a combination of non-pharmaceutical interventions can achieve the most potent effects in controlling COVID-19. Quantified analysis of the human mobility data in the U.S. also reveals the impact of social distancing in decreasing substantial case growth [30]. Furthermore, authors in [24] proposed a dynamic mobility network to simulate the spread of COVID-19. A nationwide simulation is conducted to measure the burden brought by the COVID-19 in 2020 [31] based on a model-inference approach. These studies focused on analyzing the effects of policies on human mobility or statistically modeling the dynamics. Nevertheless, the long-term co-evolution patterns between policies and human mobility and their generalization ability over time and varied contexts are less studied.

Our solutions. As current deep learning-based human mobility prediction models focus on deterministic outputs based on rich history observations [32, 33], they cannot generate probabilistic estimations of human mobility. Furthermore, considering the practical demands of policymakers, generative models, being able to learn the distribution of collected data and simulate multiple potential human mobility conditions under different policies, are more useful for human mobility estimation during COVID-19. For example, the government can formulate phased reopen plans based on the simulated human mobility response for the COVID-19 pandemic. In this paper, we show a conditional generative adversarial network [34], usually used for image generation, can be adapted to model the complex dynamics among newly confirmed cases, policies, and human mobility. Based on Figure 2, we find that almost all the cities experience an abrupt decline to a relatively slow revival phase, resonating with the COVID-19 related policies and confirmed cases. Surprisingly, the history of human mobility provides less information to estimate the unprecedented and fast-changing human mobility during COVID-19 (see Supplementary Material, extended Figure 3). Thus, instead of modeling the long-term dependencies, we focus on predicting the human mobility transition between adjacent time slots shaped by the potential COVID-19 statistics, policies, and the latest dynamic of human mobility. To be specific, we propose a policy-human mobility interplay network (PHMIN) to estimate the human mobility changes based on conditional generative adversarial network. Here, the conditions are mainly derived from the COVID-19 statistics and policies, potentially influencing human mobility. Compared with traditional prediction methods, our model can flexibly learn wide-ranging human mobility dynamics and accurately extend to multi-waves of epidemics across cities.

MATERIALS AND METHODS

Dataset and preprocessing

In this study, one year and three months anonymized human mobility data from three cities are utilized, ranging from January 1, 2020 to March 31, 2021, including Beijing (BJ), Shijiazhuang (SJZ), and Dalian (DL), China. This de-identified dataset is collected in a crowdsourced way from over 10 million smart devices opt-in uploading location reports, processed by the Westlake Institute for Data Intelligence for research purposes conforming to the Personal Information Security Specification of China (2019). Considering the privacy issues, we further aggregate the data into gridded heatmaps to represent the regional human mobility level.
Moreover, we specify the duration and intensity of each wave of COVID-19 for different cities in Figure 2 according to the official statements. The intensity of the epidemic is divided into two levels, depending on the degree of mobility restrictions, marked with blue and green parts in Figure 2, respectively. The major difference between high and low-intensity policies is whether the mobility curves reveal the weekly periods. High-intensity policies such as strict lockdown usually lead to a constant low mobility level. In contrast, median policies just result in a small drop without covering up weekly periods (i.e., normal life rhythm). From Figure 2, we can observe the similarities and variations across cities, which are highly correlated with the epidemiological situations.

Before formally formulating our problem, we provide several critical definitions.

- **Region**: The city is divided into $H \times W$ grids with equal size (900 m×600 m according to the Geohash6 standards [35]). Each grid represents a region of the city.

- **Human mobility level**: We measure the regional human mobility level $m$ via the total visits of PoIs (point of interests), including shopping malls, residential areas, and companies. Human mobility level can explain most local transmissions during COVID-19 based on existing research [24], which reveals that infections are more likely to happen in the PoIs with higher human mobility levels (i.e., population density). Therefore, each region is associated with a series of human mobility levels across the study period.

- **Human mobility map**: To explore the overall human mobility of the city, we further define the human mobility map as $\mathbf{M} \in \mathbb{R}^{H \times W}$ with each entry $m_{i,j}$ representing the human mobility level of the corresponding region.

- **COVID-19 statistics**: Based on the results in Figure 2, we identify the most direct and informative
COVID-19 policies: Many countries have taken various policies to control the COVID-19 pandemic, especially on restricting human mobility. Here we refer to the Oxford COVID-19 Government Response Tracker project [25], which collected the strength of daily policies in China with several indicators, including containment and closure policies, economic policies, and health system policies. Specifically, we focus on the policies tightly related to human mobility, such as school and workplace closing, restrictions on gatherings and internal movement, stay at home requirements, denoted as \( P \).

For a specific city, given historical and current human mobility maps \( \{ M_{t-1} ; M_t \} \) and corresponding COVID-19 statistics \( \{ C_{t-1} ; C_t ; C_{t+1} \} \) (plenty of articles have achieved the accurate real-time forecasts on newly confirmed cases [36–38]), and policies \( \{ P_{t-1} ; P_t ; P_{t+1} \} \) (can be made by policymakers in advance), we try to estimate the future human mobility map \( M_{t+1} \).

The workflow of PHMIN

As shown in Figure 4, PHMIN is designed based on the conditional generative adversarial network, which mainly consists of two components: (1) a generator including a transformer-based encoder and domain knowledge aware decoder (i.e., COVID-19 statistics and policies); (2) a discriminator to distinguish the human mobility dynamics during the COVID-19 and improve the model training.

**Generator.** The human mobility maps are essentially highly correlated on both spatial and temporal domains. However, there is neither long-term data nor stable patterns to learn from during the COVID-19 progression in our problem. Therefore, we model the human mobility changes in an incremental way shown in Figure 4A. The input of the generator is the calculated difference between two continuous human mobility maps \( \Delta M_{t-1} = M_t - M_{t-1} \), indicating the latest temporal trends on human mobility. On the other hand, the spatial features are more complicated due to the multi-scale dynamics we have mentioned in the Introduction. Therefore, we first introduce the convolution layer and transformer encoder inspired by [39] to extract the local and long-range correlation between regions, respectively. Specifically, the transformer encoder is composed of a multi-head self-attention module followed by an MLP layer, where both parts are equipped with layer-normalization and skip-connections. The feature maps \( f_0 \in \mathbb{R}^{H \times W \times C} \) derived from the convolution layer are directly flattened into length-\( H \times W \) sequence of \( C \)-dimension embedded tokens. Then transformer encoder can recursively calculate the correlations between each pair of tokens, which has stronger representation capability without locally inductive bias. The processed 1D sequence of tokens is reshaped back into the 2D feature map \( f_1 \in \mathbb{R}^{H \times W \times C} \), serving as the output of encoder in the generator. The encoded feature is then concatenated with the COVID-19 condition feature map to jointly estimate the \( \Delta \tilde{M} \), via the decoder.

**Domain knowledge adaptation.** Another critical component in PHMIN is the domain knowledge adaptation module, which aims to fuse COVID-19 related statistics and policies as conditions. However, the conditions here are not as explicit as the class labels when generating images. For example, when going through a wave of epidemics completely from decline to revival, we will encounter a pair of similar human mobility heatmaps with opposite trends. This phenomenon enables us to provide conditions with direction information to guide the evolution of human mobility. Similar to the generator’s input, the first-order difference of confirmed cases and policies can also provide rich information on the trends. For example, a
Figure 4  The framework of PHMIN. The framework mainly consists of two parts. (A) The generator for human mobility estimation. The original input contains the human mobility map of the last two time steps. The domain knowledge from COVID-19 statistics and policies is embedded and adapted to guide the estimation of future human mobility. (B) The discriminator is implemented to distinguish whether the human mobility dynamics is consistent with the period of COVID-19 or not.
sudden increase in the newly confirmed cases usually leads to more strict mobility restrictions. By contrast, a decline in the number of confirmed cases is likely to cause people to cease their vigilance along with more frequent mobility. When the confirmed cases return to zero and last for two weeks, the mobile restrictions will be removed in the corresponding city of China [40]. Therefore, the changes of newly confirmed cases or policies are more valuable, shaping people’s confidence towards the future and implicitly impacting people’s mobility intention. Furthermore, considering the different scales and population bases of cities, directly feeding the absolute value of the difference is not applicable. We introduce a dense network to turn it into latent vectors \( C \in \mathbb{R}^{H \times W \times C_h} \). Then we adopt a gating fusion as the activation function of spatial-temporal features, which uses \( C \) to activate features \( f_1 \) as \( f'_1 = \sigma(C \odot f_1) \). Considering the randomness and unknown factors during this process, we further add the noise vector \( N \in \mathbb{R}^{H \times W \times C_0} \) concatenated with the latent vector. This part serves as the domain knowledge driving the evolution of human mobility. Finally, the features derived from recent human mobility changes, COVID-19 statistics, and policies jointly estimate the future human mobility \( \Delta M_n \). A skip connection is constructed across the generator to produce the estimation for next time step \( M_{t+1} = M_t + \Delta \hat{M}_t \). In this way, the complex dynamics of human mobility is modeled progressively.

**Discriminator.** Figure 4B illustrates the detailed structure of the discriminator. The inputs to the discriminator are human mobility changes rather than generated fluctuating human mobility maps, which makes our learning process more accessible and stable. Specifically, there are two types of inputs for the discriminator, i.e., generated human mobility changes with label fake and calculated real human mobility changes with label real. The discriminator is trained to predict the label of the human mobility map, indicating whether the generated human mobility map is consistent with real distribution.

**Optimization.** Our model is trained in an adversarial way, where the generator is trained to simulate the realistic human mobility response, and the discriminator aims to judge the correctness of the generated samples. The adversarial process essentially plays a min-max two-player game with a unique optimal solution when the generator can produce human mobility maps, effectively confusing the discriminator. Therefore, our loss function contains an estimation loss from the generator and an adversarial loss from the discriminator. Given the input human mobility maps \( M_t, M_{t-1} \), we can get the pixel-wise mean square error (MSE) loss between estimated human mobility map \( \tilde{M}_{t+1} = G(M_t, M_{t-1}, C, P, N) \) and the ground truth \( M_{t+1} \). Furthermore, some suburbs and natural terrains (e.g., rivers, seas, and mountains) are desolate and uninhabited, whose samples are more like noise than real human mobility patterns. We further introduce a mask matrix \( K \in \mathbb{R}^{H \times W} \) to reduce the negative effects brought by noisy samples, whose elements are binary with one indicating regions with available data and zero for uncertain regions. Thus, we can calculate the masked loss for the generator:

\[
L_G = \frac{1}{\|K\|_1} \| (\tilde{M}_{t+1} - M_{t+1}) \odot K \|_F^2,
\]

where \( \odot \) implies the element-wise multiplication for matrix. \( \| \cdot \|_1 \) and \( \| \cdot \|_F \) stand for the \( L_1 \) and Frobenius norm, respectively. The mask matrix \( K \) provides supplementary information associated with the real-world sampled data distribution. Many studies [41] have pointed out that adding a discriminator to distinguish the generated samples from the real can effectively improve the learning process by exerting a regularization as follows:

\[
L_D = E_{M_{t+1}} \log D(M_{t+1}, M_t) + E_{N_{t+1}} \log(1 - D(G(M_t, M_{t-1}, C, N)))
\]
Finally, combining the losses from both the generator and discriminator, the adversarial loss can be written as
\[ \min_G \max_D L_G + \lambda L_D, \]  
(3)
where the parameter \( \lambda \) is the weight that controls the trade-off between two objectives. We seek the saddle point by alternatively updating the parameters of the generator and the discriminator with Adam optimizer [42]. Besides, the discriminator classifier will not work during the test phase once the model is well-trained.

**Experimental settings**

The whole dataset is divided into seven sub-datasets based on the specific city-wave combination, i.e., BJ-1, BJ-2, DL-1, DL-2, DL-3, SJZ-1, SJZ-2. Naturally, we can take a pair of sub-datasets as the training and test set (i.e., source and target dataset from the point of model generalization), where the time of the training set should be earlier or simultaneous compared with the test set time considering the practical constraints.

**Metrics.** Considering both absolute and relative deviations of the estimation, two metrics are taken for comprehensive model evaluations, including mean absolute error (MAE) and mean absolute percentage error (MAPE). Moreover, the mask matrix \( K \) is also introduced to handle the data missing and uncertainty. Therefore, the metrics are modified as follows:
\[
\text{MAE} = \frac{1}{z} \sum_{i=1}^{z} \frac{1}{\| K \|_{1,1}} \times \| (\hat{M}_i^f - M_i^f) \odot K \|_{1,1}, \\
\text{MAPE} = \frac{1}{z} \sum_{i=1}^{z} \frac{1}{\| K \|_{1,1}} \times \| (\hat{M}_i^f - M_i^f) \odot M_i^f \odot K_i^f \|_{1,1},
\]  
(4)
where \( z \) is the number of samples. \( \| \cdot \|_{1,1} \) and \( \| \cdot \|_{F} \) imply the \( L_{1,1} \) and Frobenius norm, respectively. \( \odot \) and \( \oslash \) stand for the element-wise multiplication and division for the matrix. Generally speaking, smaller values of metrics suggest a better performance.

**Baselines.** We first introduce three baseline methods for comparison as follows:
- Historical average (HA): A heuristic method simply taking the average of the same time interval. In this article, we calculate the average of the last two time steps.
- ARIMA [43]: A classical autoregressive integrated moving average model for the time series forecast.
- Conditional GAN (cGAN) [34]: A GAN-based model directly combines the condition with noise without considering the difference between time steps.
- DeepST [33]: A deep learning based spatial-temporal prediction model.

**Model variants.** To explore the effects of designed modules, we further conduct experiments on the following methods:
- PHMIN: The proposed model.
- PHMIN-rm: Remove the proposed mask matrix from our model.
- PHMIN-rcp: Remove both the policies and COVID-19 statistics conditions from our model.
- PHMIN-rp: Remove both the policies conditions from our model.
RESULTS AND DISCUSSION

Multiple experimental settings indicate the generalization ability of our model

Considering there are three cities with seven waves of COVID-19 and two types of intensity, we divide the experiments into three groups to analyze the results hierarchically under (1) inter-city similar intensity; (2) inter-city different intensity; (3) intra-city similar/different intensity. These experiments emphasize a fundamental question: whether our model is generalizable in different contexts. We will answer this question in detail in the following. The bold results in the following tables indicate the best performance under different experimental settings.

**Inter-city similar intensity.** Based on the results shown in Table 1, we have several observations as follows.

- Generally speaking, our model achieves the best performance compared with baselines, which proves the excellent generalization ability of our model across cities. Specifically, the relatively simple HA and ARIMA models show better performance than DeepST and GAN, to some extent implying that the most valuable information in our problem is associated with the latest situations on human mobility. Furthermore, the conditional GAN slightly outperforms the DeepST due to its advantage in modeling unknown factors of human mobility in a generative manner. DeepST, on the other hand, can provide a deterministic prediction based on rich history observations, which is not suitable for our scenario.

- Given the same test city, the model derived from different training cities results in diverse performance. When testing on DL1, SJZ1, and SJZ2, the model trained based on the BJ1 shows better results than other cities. This can be attributed to the best data quality from BJ, which has more available samples with a high population density.

- Geographical similarity potentially influences the effects of model generalization across cities. The model trained based on the DL1 usually leads to worse performance. Take the results on DL1-BJ1, DL1-SJZ1, and DL1-SJZ2, for example, their results are close to ARIMA (with better MAEs while worse MAPEs). In fact, DL is surrounded by the ocean leading to irregular urban areas, while the BJ and SJZ are very regular with checkerboard layouts. The gaps in spatial distribution are likely to make the model generalization

![Table 1](image)

**Table 1**  Inter-city similar intensity experiments

<table>
<thead>
<tr>
<th>Model setting</th>
<th>HA</th>
<th>ARIMA</th>
<th>cGAN</th>
<th>DeepST</th>
<th>PHMIN</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>MAE</td>
<td>MAPE</td>
<td>MAE</td>
<td>MAE</td>
<td>MAE</td>
</tr>
<tr>
<td>BJ1-DL1</td>
<td>1260</td>
<td>0.111</td>
<td>1013</td>
<td>0.086</td>
<td>2639</td>
</tr>
<tr>
<td>SJZ1-DL1</td>
<td>1260</td>
<td>0.111</td>
<td>1013</td>
<td>0.086</td>
<td>1782</td>
</tr>
<tr>
<td>DL1-BJ1</td>
<td>10305</td>
<td>0.369</td>
<td>6558</td>
<td>0.177</td>
<td>38316</td>
</tr>
<tr>
<td>SJZ1-BJ1</td>
<td>10305</td>
<td>0.369</td>
<td>6558</td>
<td>0.177</td>
<td>22947</td>
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<tr>
<td>BJ1-SJZ1</td>
<td>1824</td>
<td>0.201</td>
<td>1138</td>
<td>0.115</td>
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<tr>
<td>DL1-SJZ1</td>
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<td>0.201</td>
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<td>1090</td>
<td>0.064</td>
<td>1397</td>
</tr>
<tr>
<td>BJ2-DL3</td>
<td>1366</td>
<td>0.093</td>
<td>1012</td>
<td>0.077</td>
<td>1439</td>
</tr>
</tbody>
</table>

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harder.

**Inter-city different intensity.** To investigate the performance between epidemic waves with different intensity, i.e., high to median and median to high, we further conduct experiments shown in Table 2 demonstrating the following.

- In most instances, our model still performs better than the baselines. However, for the same test city, the overall performance is worse than the model obtained from the similar intensity in Table 1. This illustrates that compared with the diverse urban contexts, the intensity of the epidemic is a more critical indicator affecting the generalization ability of our model.

- The model trained from DL still performs poorly on other cities (e.g., DL1-BJ2 and DL2-SJZ2), which again illustrates the importance of geographical similarity. Additionally, the double gaps in both geography and intensity lead to even worse results than the baseline ARIMA under DL2-SJZ2.

**Intra-city similar/different intensity.** Intuitively, the intra-city experiments, i.e., multi-waves COVID-19 within the same city, should share more common patterns. However, the results in Table 3 reveal more insights on this process.

- Our model outperforms the baselines in all intra-city experiments. Besides, three groups of experiments, including SJZ1-SJZ2, DL2-DL3, and BJ1-BJ2, reach their best performance respectively compared with results in Tables 1 and 2, which implies the intra-city gaps might be smaller than previous conditions.

- The exception occurs in DL1-DL2 and DL1-DL3, whose results are even worse than BJ2-DL2 and BJ2-DL3, respectively. This can be attributed to BJ2, DL2, and DL3, although in different cities, they share similar intensity. Comparing results between DL2-DL3 and DL1-DL3, we deduce that our model generalizes better between similar intensity within the same city.

### Table 2  Inter-city different intensity experiments

<table>
<thead>
<tr>
<th>Model setting</th>
<th>HA MAE</th>
<th>MAPE</th>
<th>ARIMA MAE</th>
<th>MAPE</th>
<th>cGAN MAE</th>
<th>MAPE</th>
<th>DeepST MAE</th>
<th>MAPE</th>
<th>PHMIN MAE</th>
<th>MAPE</th>
</tr>
</thead>
<tbody>
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<td>1090</td>
<td>0.064</td>
<td>3923</td>
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<td>5131</td>
<td>0.301</td>
<td>777</td>
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</tr>
<tr>
<td>SJZ1-DL2</td>
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<td>1090</td>
<td>0.064</td>
<td>2374</td>
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<td>1012</td>
<td>0.077</td>
<td>3478</td>
<td>0.205</td>
<td>5619</td>
<td>0.309</td>
<td>981</td>
<td>0.066</td>
</tr>
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### Table 3  Intra-city similar/different intensity experiments

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Ablation study on model variants

In this part, we aim to investigate the effects of modules via ablation studies. Specifically, we focus on the domain knowledge adaptation module by gradually removing the designed modules from the original models, i.e., mask matrix, knowledge from policy, or confirmed cases. We aggregate the experiments under different model variants shown in Table 4, from which we have several observations as follows.

- The model PHMIN-rcp shows worse performance than PHMIN-rp and PHMIN, which illustrates that the change of policies and confirmed cases provide useful prior knowledge to enhance the performance. More specifically, for the settings with similar intensity (i.e., from BJ1-DL1 to BJ2-DL3, SJZ1-SJZ2, and DL2-DL3), PHMIN-rp slightly outperforms PHMIN in some experiments. Removing the mask matrix leads to worse results under all the circumstances, which illustrates its effectiveness in mitigating the negative effects brought by regions with low-quality samples.

- The best results under each setting are achieved by either PHMIN-rp or PHMIN, implying the policy information is not always beneficial. Especially in the first wave of COVID-19, all the cities implement stringent policies, resulting in a comparable performance without policy information. Nevertheless, when it comes to different intensities, PHMIN shows an overwhelming advantage over PHMIN-rp in almost all

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the cases (i.e., from BJ1-DL2 to DL2-SJZ2, from BJ1-BJ2 to DL1-DL3). These results can be explained by the pattern of confirmed cases that are very distinguished with different intensities, making the model generalization solely depending on confirmed cases (i.e., PHMIN-rp) unreliable. On the other side, policies are more universal across multi-waves of COVID-19, considering that the Chinese government will revert the policy to a high or very high level even just local transmissions are identified.

- We further visualize the human mobility changes with/without domain knowledge in BJ1 to obtain more insights. Figure 5A is the human mobility map before lockdown policy in the first wave of COVID-19 in Beijing. After adopting the policy, the human mobility map of BJ turns into Figure 5C, which is close to the estimation of our model in Figure 5D. If there is no COVID-19 related knowledge, the estimated human mobility will hold a relatively high level like Figure 5A. These results prove the effectiveness of COVID-19 knowledge adaptation.

Analysis of single-step and multi-step estimation

The experiments above illustrate the overall performances of our model, generalizing across cities and multiple waves of epidemics. In practice, we also care about how accurately our model can approximate the real data during COVID-19, i.e., prediction of each time step and the general trends from decline to revival. Therefore, we further conduct multiple experiments and visualize the generated results for three cities in Figure 5. We average the mobility of generated results to better reflect the tendency during each wave of COVID-19, where the shaded regions denote the variance over sampled parameters and stochastic realizations for each time step. Furthermore, our model can also recurrently generate multi-step estimations by taking the output of the model as the input for predicting the next time step. In practice, we are interested in whether multi-step estimation can predict long-term trends while mitigating accumulated errors. The multi-step estimations are also shown in Figure 5, from which we notice the following.

- In general, the results of single-step estimations are very close to the real trends of human mobility patterns, which accurately predict the drop and revival point during a wave of the epidemic. Multi-step estimations can still depict the trends of COVID-19, although they perform worse than single-step estimations on accuracy due to the accumulated errors. This proves that our model can handle the scenario of multi-step prediction.

- The errors of each time step are not uniform, where the decline stage of each wave is usually associated with higher errors than the revival stage. This can be attributed to fewer samples during the decline stage compared with relatively longer revival stages, making it difficult to learn stable patterns.

- There are still some drawbacks of the generated results. The transitions at the bottom of some curves are not as smooth as the real-world process, such as the BJ1 and BJ2 in Figures 5A and 5B. This might be that the transition stage in BJ is short and drastic with a large population base, resulting in a larger momentum of mobility change compared with other cities.

Case study on human mobility in the U.S.

To further verify the effectiveness of the proposed model, we also conduct additional experiments on the U.S. datasets. We obtain the human mobility datasets from [44], where we select two major cities on the east coast of the U.S., i.e., Boston (BOS) and Philadelphia (PA). Specifically, Philadelphia is an inland city
Figure 5  Estimated human mobility with single/multi-step settings across multiple cities. (A) BJ1, (B) BJ2, (C) SJZ1, (D) SJZ2, (E) DL1, (F) DL2, (G) DL3.
similar to Beijing or Shijiazhuang in China, while Boston is a seaside city similar to Dalian, China. The period ranges from March 2, 2020 to July 5, 2020. Moreover, considering that the crowd distribution in the U.S. is relatively sparser than in China, the aggregated human mobility map in the U.S. is associated with a bigger size (about 2.7 km × 1.8 km). We further investigate the inter-city human mobility estimation between the two cities in Table 5. The results reveal that our model still outperforms all the baselines for the human mobility datasets from the U.S., which can be attributed to the similar human mobility patterns in the early stage of the COVID-19. The naive heuristic method HA also achieves a better performance than other baselines but is not as good as ours, which illustrates that the historical average is a good indicator for human mobility during COVID-19 with seemingly unusual patterns.

CONCLUSION

Human behaviors, especially spatial-temporal mobility patterns, have become the critical determinant of COVID-19 emergence. With a detailed analysis of multiple epidemics in three cities, we identify the vital indicators shaping human mobility, i.e., COVID-19 policies and statistics. Thus, we propose the model PHMIN to estimate human mobility via modeling the influence of COVID-19 policies and statistics. Our model shows excellent generalization ability in both inter- and intra-city experiments. The results reveal that the changes in human mobility share universal patterns during epidemics. Furthermore, our model can also recurrently produce multi-step estimations, allowing the governments to evaluate the influence of different policies. They are helpful in managing and controlling mobility during a pandemic or other disaster events.

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Author contributions

J.C. and S.H. conceived the study. K.L., Y.X., and C.L. performed the computational analysis. D.T. and F.H. analyzed the results. Y.F. provided and analyzed the human mobility data. K.L. wrote the manuscript with C.L., S.H., and F.H. All authors reviewed and revised the manuscript.

Conflict of interest

The authors declare that they have no conflict of interest.

Table 5  Experiments on the U.S. cities

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Supplementary information
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